#### Analysis Report for Preparation of 2009 Culebra Potentiometric Surface Contour Map

Revision 1

Task Number: 1.4.2.3

Manager, Repository Performance Department

#### **Table of Contents**

1	Intr	ntroduction3				
2		entific Approach				
	2.1	Overview				
	2.2	Creating Ensemble Average MODFLOW Simulation	6			
	2.3	Boundary Conditions	6			
	2.4	PEST Calibration of Averaged MODFLOW Model to Observations	7			
	2.5	Figures Generated from Calibrated MODFLOW Model	9			
3	Res	ults	10			
	3.1	Freshwater Head Contours	10			
	3.2	Particle Track	12			
	3.3	Measured vs. Modeled Fit	13			
4	Refe	erences	17			
5	Run	Control Narrative	18			
Α	Run	Control Appendix	24			
	A-1	Input Files	24			
	A-2	Output Files	25			
	A-3	Directory Listings	26			
	A-4	Script Source Listings	28			

#### 1 Introduction

This report documents the preparation of a potentiometric contour map and particle track for the Culebra Member of the Rustler Formation in the vicinity of the Waste Isolation Pilot Plant (WIPP), for inclusion in the 2010 Annual Site Environmental Report (ASER). The driver for this analysis is the draft of the Stipulated Final Order sent to the New Mexico Environment Department (NMED) on May 28, 2009 (Moody, 2009). This Analysis Report follows the procedure laid out in SP 09-09 (Kuhlman, 2009b), which is based upon this NMED driver. This report is a revision of Kuhlman (2009a), where the same analysis is being performed on June 2009 data, rather than September, 2008 data.

Beginning with the ensemble of 100 calibrated MODFLOW transmissivity (T), horizontal anisotropy (A), and areal recharge (R) fields (Hart et al., 2009) used in WIPP performance assessment (PA), 3 average parameter fields are used as input to MODFLOW to simulate freshwater heads within and around the WIPP land withdrawal boundary (LWB). PEST is used to adjust a subset of the boundary conditions in the ensemble-average model to obtain the best-fit match between the observed freshwater heads from June 2009 and the model-predicted heads. The output of the averaged, PEST-calibrated MODFLOW model is both contoured and used to compute an advective particle track forward from the WIPP waste handling shaft.

#### 2 Scientific Approach

#### 2.1 Overview

Steady-state groundwater flow simulations are carried out using much the same software and approach used in the analysis report for AP-114 Task 7 (Hart et al., 2009) to create the calibrated fields used as inputs – see Table 1 for a summary of all software used in this analysis. The MODFLOW parameter fields (including transmissivity (T), anisotropy (A), and recharge (R)) used here are an ensemble average of the Culebra parameter fields used for WIPP PA in the CRA-2009 performance assessment baseline calculations (PABC). To clearly distinguish between the two MODFLOW models, the original MODFLOW model, which consists of 100 realizations of calibrated parameter fields (Hart et al., 2009), will be referred to as the "PA MODFLOW model". The model derived here from the PA MODFLOW model, used to construct the resulting contour map and particle track, is referred to as the "averaged MODFLOW model". The calibrated model T, A and R input fields, model boundary conditions, and other model input files are appropriately averaged across all 100 calibrated realizations to produce a single averaged steady-state MODFLOW flow model that can be used to predict regional Culebra groundwater flow across the WIPP site.

The calibration process that resulted in the 100 model realizations of the PA MODFLOW model used PEST to adjust spatially variable model parameters, while assuming fixed MODFLOW boundary conditions. The calibration targets for the PA MODFLOW model were both snapshots of undisturbed heads across the site and transient head responses to large-scale pumping tests. Hart et al. (2009) describe the forward model setup and PEST calibration effort for the CRA-2009 PABC. An analogous but much simpler process is used in the averaged MODFLOW model; here PEST is used to modify a subset of the MODFLOW boundary conditions (see boundaries marked in red on Figure 1). The calibration targets for PEST associated with the average MODFLOW model are the observed June 2009 freshwater heads at Culebra monitoring wells. Boundary conditions are modified while holding spatially variable model parameters (T, A, and R) constant; in the calibration of the PA MODFLOW model, the boundary conditions were fixed, while adjusting the spatially variable parameters.



Table 1. Software used

Software	Version	Description		
MODFLOW-2000	1.6	Flow model	Acquired; qualified under NP 19-1 (Harbaugh et al., 2000)	
PEST	9.11	Inverse model	Developed; qualified under NP 19-1 (Doherty, 2002)	
DTRKMF	1.00	Particle tracker	Developed; qualified under NP 19-1	
Golden Software Surfer	9	Contouring	Commercial off the shelf	
Gnuplot	4.2	Plotting	Commercial off the shelf	
Microsoft Excel	2007	Plotting, Regression	Commercial off the shelf	
Python	2.3.4	Scripting Language	Commercial off the shelf	
CorpsCon6	6.01	Coordinate Conversion	Commercial off the shelf	

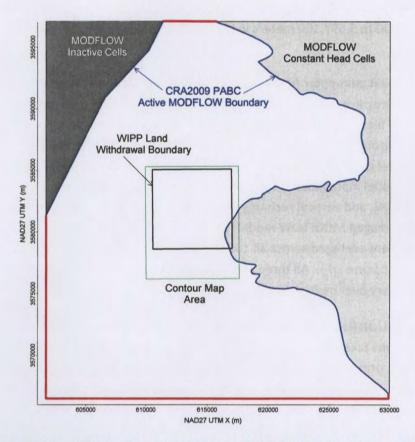


Figure 1. MODFLOW-2000 model domain, adjusted boundary conditions shown in red, contour area outlined in green.

The resulting heads from the PEST-calibrated ensemble-average flow model are contoured over an area surrounding the WIPP site using Surfer (a subset of the complete MODFLOW model domain – see the green rectangle surrounding the WIPP LWB in Figure 1). The track made by a conservative (i.e., non-

dispersive and non-reactive) particle released from the waste handling shaft to the WIPP land withdrawal boundary is computed from the resulting flow field in MODFLOW using DTRKMF, and also plotted with Surfer. Scatter plot statistics summarizing the fit of the PEST-calibrated model to the observed freshwater head at Culebra monitoring wells are created in Gnuplot and Excel. MODFLOW, PEST, DTRKMF, and the Bash and Python scripts written for this work were executed on the PA Linux cluster (alice.sandia.gov), while the commercial-off-the-shelf software Surfer, Gnuplot and Excel were executed on a Windows XP desktop computer with an Intel Xeon CPU.

#### 2.2 Creating Ensemble Average MODFLOW Simulation

An ensemble-average MODFLOW model is used to compute both the freshwater head and flow vectors across the model domain; the heads are then contoured and the cell-by-cell flow vectors are used to compute particle tracks. The ensemble-averaged inputs are used to create a single average simulation that produces a single output, rather than averaging the 100 individual outputs of the Culebra flow model used for WIPP PA.

The MODFLOW model grid is a single layer, comprised of 307 rows and 284 columns, each model cell being 100 meters square. The modeling area spans 601,700 to 630,000 meters in the east-west direction, and 3,566,500 to 3,597,100 meters in the north-south direction, both in UTM NAD27 coordinates (zone 13).

The calibrated T, A, and R parameter fields from the PA MODFLOW model were checked out of the CVS repository using the <code>checkout\_average\_run\_modflow.sh</code> script (all scripts are listed completely in the Appendix; input files are available on the attached media). The model inputs can be divided into two groups. The first group is the model inputs that are the same across all 100 calibrated realizations; these include the model grid definition, the boundary conditions, and the model solver parameters. The second group is the model inputs that are different for each realization; these include transmissivity (T), horizontal anisotropy (A), and vertical recharge (R). The constant model inputs in the first group are used directly in the averaged MODFLOW model (checked out from the CVS repository), while the inputs in the second group were averaged across all 100 calibrated model realizations using the Python script <code>average\_realizations.py</code>. All three averaged parameters were log transformed before being averaged, since they vary over multiple orders of magnitude.

#### 2.3 **Boundary Conditions**

The boundary conditions taken from the PA MODFLOW model are used as the baseline condition from which PEST calibration proceeds. There are two types of boundary conditions in both MODFLOW models. The first type of condition includes geologic or hydrologic boundaries, which correspond to known physical features in the flow domain. The no-flow boundary along the axis of Nash Draw is a hydrologic boundary (i.e., the boundary along the dark gray region in Figure 1). Also, the constant-head boundary along the halite margin corresponds to a geologic boundary (i.e., the eastern irregular boundary adjoining the light gray region in Figure 1).



Physical boundaries are believed to be well known, and are not adjusted in the PEST calibration. The second type of boundary condition includes the constant-head cells along the rest of the model domain; the linear southern, southwestern, and northern boundaries that coincide with the rectangular frame surrounding the model domain are all of this type (shown as a heavy red line in Figure 1). The value of specified head used along this second boundary type is adjusted in the PEST calibration process.

The Python script boundary\_types.py is used to distinguish between the two different types of specified head boundary conditions based on the specified head value used in the PA MODFLOW model. All constant-head cells (specified by a value of -1 in the MODFLOW IBOUND array from the PA MODFLOW model) that have a starting head value greater than 1000 m (corresponding to the land surface) are left fixed and not adjusted in the PEST optimization. The remaining constant-head cells are distinguished by setting their IBOUND array value to -2 (which is still interpreted as a constant-head value by MODFLOW, but allows simpler discrimination between boundary conditions in scripts elsewhere).

Using the output from boundary\_types.py, the Python script surface\_02\_extrapolate.py computes the heads at active (IBOUND=1) and adjustable constant-head boundary condition cells (IBOUND=-2), given parameter values for the surface to extrapolate.

#### 2.4 PEST Calibration of Averaged MODFLOW Model to Observations

There are three major types of inputs to PEST. The first type of input includes the set of observed June 2009 freshwater head values used as targets for the PEST calibration. The second class of inputs includes the entire MODFLOW model setup derived from the PA MODFLOW model and described in the previous section, along with any pre- or post-processing scripts or programs needed; this comprises the forward model that PEST runs repeatedly to estimate sensitivities of model outputs to model inputs. The third type of input includes the PEST configuration files, which include parameter and observation groups, indicating which parameters in the MODFLOW model will be adjusted in the inverse simulation.

Freshwater head values used as targets for the PEST calibration were collected in June 2009 (Waterson, 2010) and are summarized in Table 2.



Table 2. Calibration targets used in PEST, from Watterson (2010).

Well I.D.	Date	Adjusted Freshwater Head	Adjusted Freshwater Head	Density Used (g/cm³)
		(ft amsl)	(m amsl)	
AEC-7	06/09/09	3064.59	934.09	1.078
C-2737 (PIP)	06/11/09	3023.32	921.51	1.029
ERDA-9	06/11/09	3033.59	924.64	1.067
H-2b2	06/10/09	3043.09	927.53	1.000
H-3b2	06/11/09	3013.69	918.57	1.038
H-4b	06/09/09	3005.97	916.22	1.013
H-5b	06/09/09	3081.40	939.21	1.093
H-6bR	06/08/09	3070.79	935.98	1.033
H-7b1	06/08/09	2998.35	913.90	1.000
H-9c (PIP)	06/09/09	2996.27	913.26	1.003
H-10c	06/09/09	3024.23	921.78	1.001
H-11b4	06/09/09	3006.94	916.52	1.062
H-12	06/09/09	3007.34	916.64	1.096
H-15R	06/10/09	3022.22	921.17	1.130
H-16	06/11/09	3050.00	929.64	1.039
H-17	06/09/09	3003.56	915.48	1.120
H-19b0	06/11/09	3017.73	919.80	1.075
IMC-461	06/08/09	3047.07	928.75	1.019
SNL-1	06/08/09	3084.61	940.19	1.032
SNL-2	06/08/09	3074.36	937.07	1.015
SNL-3	06/08/09	3082.29	939.48	1.029
SNL-5	06/08/09	3077.12	937.91	1.012
SNL-6	06/10/09	2971.33	905.66	1.253
SNL-8	06/09/09	3055.63	931.36	1.104
SNL-9	06/08/09	3057.38	931.89	1.026
SNL-10	06/08/09	3056.29	931.56	1.013
SNL-12	06/09/09	3004.22	915.69	1.011
SNL-13	06/08/09	3012.75	918.29	1.028
SNL-14	06/09/09	3005.56	916.09	1.048
SNL-15	06/09/09	2937.74	895.42	1.232
SNL-16	06/08/09	3010.83	917.70	1.023
SNL-17A	06/09/09	3006.87	916.49	1.007
SNL-18	06/08/09	3077.16	937.92	1.011
SNL-19	06/08/09	3073.30	936.74	1.008
WIPP-11	06/10/09	3082.30	939.49	1.035
WIPP-13	06/10/09	3081.40	939.21	1.055
WIPP-19	06/09/09	3063.24	933.68	1.046
WIPP-25 (PIP)	06/11/09	3068.52	935.29	1.010
WQSP-1	06/10/09	3077.17	937.92	1.048
WQSP-2	06/10/09	3085.57	940.48	1.048
WQSP-3	06/09/09	3073.79	936.89	1.144
WQSP-4	06/10/09	3015.58	919.15	1.074
WQSP-5	06/10/09	3013.46	918.50	1.025
WQSP-6	06/10/09	3025.61	922.21	1.015

To minimize the number of estimable parameters, and to ensure a degree of smoothness in the constant-head boundary condition values, a parametric surface is used to extrapolate the heads to the



estimable boundary conditions. The surface is of the same form described in the analysis report for AP-114 Task 7. The parametric surface is given by the following equation:

$$h_{x,y} = A + B * (y + D * \text{sign}(y) * \text{abs}(y)^{exponent}) + C(E * x^3 + F * x^2 - x)$$

where sign(y) is the function returning 1 for y>0, -1 for y<0 and 0 for y=0 and x and y are coordinates scaled to the range  $-1 \le \{x,y\} \le 1$ . In Hart et al. (2009), the values A=928.0, B=8.0, C=1.2, D=1.0, exponent=0.5, E=1.0, and F=-1.0 are used with the above equation.

PEST was then used to estimate the values of parameters A,B,C,D,E,F, and exponent given the observed heads in Table 2. The Python script surface\_02\_extrapolate.py was used to compute the MODFLOW starting head input file (which is also used to specify the constant-head values) from the parameters A-F and exponent. Each forward run of the forward model corresponded to a call to the Bash script run\_02\_model. This script called the surface\_02\_extrapolate.py script, the MODFLOW-2000 v1.6 executable, and the qualified PEST utility mod2obs.exe, which is used to extract and interpolate model-predicted heads from the MODFLOW output files at observation well locations.

The PEST-specific input files (the third type of input) were generated from the observed heads using the Python script create\_pest\_02\_input.py. The PEST input files include the instruction file (how to read the model output), the template files (how to write the model input files), and the PEST control file (listing the ranges and initial values for the estimable parameters and the weights associated with observations).

#### 2.5 Figures Generated from Calibrated MODFLOW Model

The MODFLOW model is run predictively using the ensemble-averaged model parameters, along with the PEST-calibrated boundary conditions. The resulting cell-by-cell flow budget is then used by DTRKMF to compute a particle track from the waste handling shaft to at least the edge of the WIPP land withdrawal boundary. The Python script convert\_dtrkmf\_output\_for\_surfer.py converts the IJK cell-based results of DTRKMF into a UTM x and y coordinate system, saving the results in the Surfer blanking file format to facilitate plotting with Surfer. The heads in the binary MODFLOW output file are converted to an ASCII Surfer grid format using the Python script head bin2ascii.py.

The resulting particle track and contours of the model-predicted head are plotted using Surfer 9 for an area including the WIPP land withdrawal boundary, similar to the region shown in previous versions of the ASER (e.g., see Figure 6.11 in DOE (2008)), see green outline in Figure 1. The modeled heads extracted from the MODFLOW output by mod2obs.exe are then merged into a common file for plotting using the Python script merge\_observed\_modeled\_heads.py.

#### 3 Results

#### 3.1 Freshwater Head Contours

The model-generated freshwater head contours in Figure 2 and Figure 3 show the known characteristics of groundwater flow in the Culebra at the WIPP site. There is a roughly east-west trending band of steeper gradients, corresponding to known lower transmissivities. The uncontoured region in the eastern part of the figure corresponds to the portion of the Culebra that is located stratigraphically between halite in other members of the Rustler Formation (Tamarisk Member above and Los Medaños Member below). This region east of the "halite margin" is represented as having high head but extremely low permeability, essentially serving as a no-flow boundary in this area.

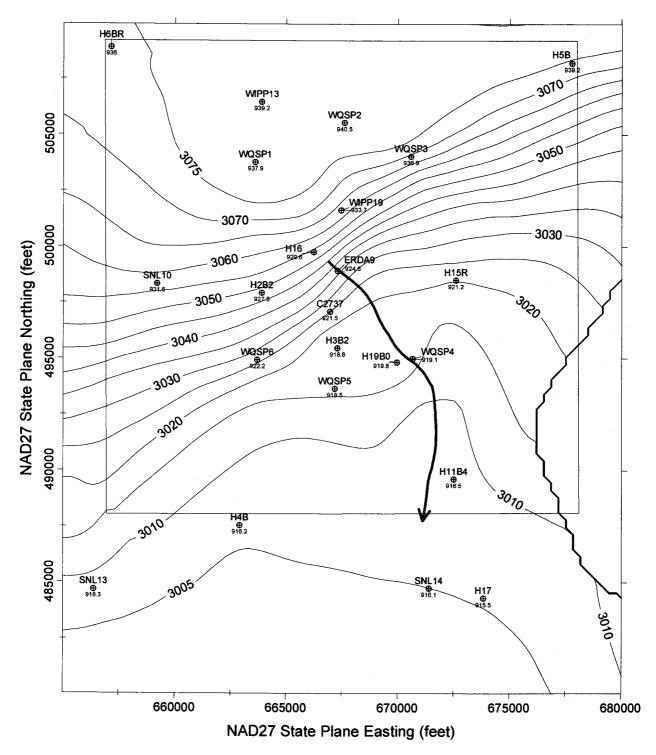


Figure 2. Model-generated June 2009 freshwater head contours with observed head listed at each well (5-foot contour interval) with blue water particle track from waste handling shaft to WIPP LWB

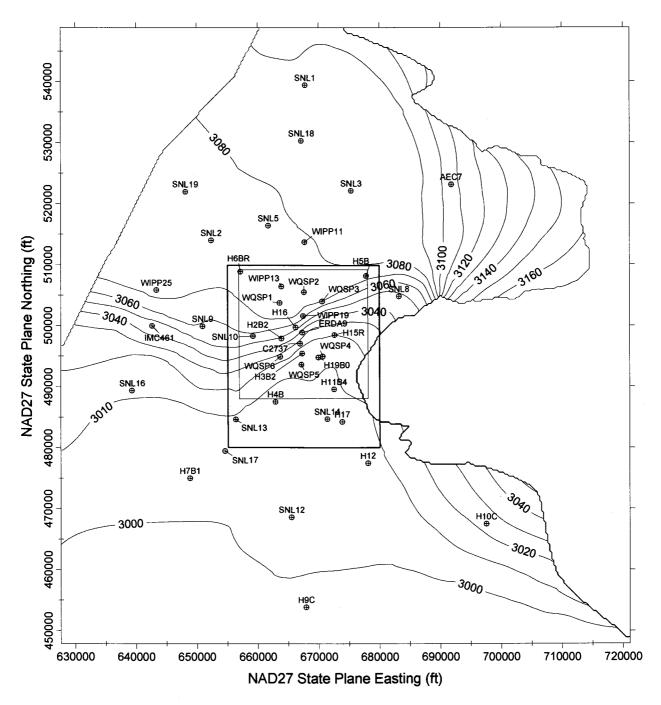


Figure 3. MODFLOW-modeled heads for entire model domain (10-foot contour interval). Green rectangle indicates region contoured in Figure 2, black square is WIPP LWB.

#### 3.2 Particle Track

The heavy blue line in Figure 2 shows the DTRKMF-predicted path a water particle would take through the Culebra from the coordinates corresponding to the WIPP waste handling shaft to the land withdrawal boundary (a computed path length of 4.089 km). Assuming a thickness of 4 m for the transmissive portion of the Culebra and a constant porosity of 16%, the travel time to the WIPP LWB is

5,900 years (output from DTRKMF is adjusted from a 7.75-m Culebra thickness), for an average velocity of 0.69 m/yr.

#### 3.3 Measured vs. Modeled Fit

The scatter plot in Figure 4 shows measured and modeled freshwater heads at the observation locations used in the PEST calibration. The observations are divided into three groups, based on proximity to the WIPP site. Wells within the LWB are represented by red crosses, wells outside but within 3 km of the LWB are represented with green "x"s, and other wells within the MODFLOW model domain but distant from the WIPP site are given by a blue asterisk. These groupings were utilized in the PEST calibration; higher weights (2.5) were given to wells inside the LWB, and lower weights (0.4) were given to wells distant to the WIPP site, while wells in the middle received an intermediate weight (1.0). Additional observations representing the average heads north of the LWB and south of the LWB were used to help prevent over-smoothing of the estimated results across the LWB. This allowed PEST to improve the fit of the model to observed heads inside the area contoured in Figure 2, at the expense of fitting wells closer to the boundary conditions (i.e., wells not shown in Figure 2).



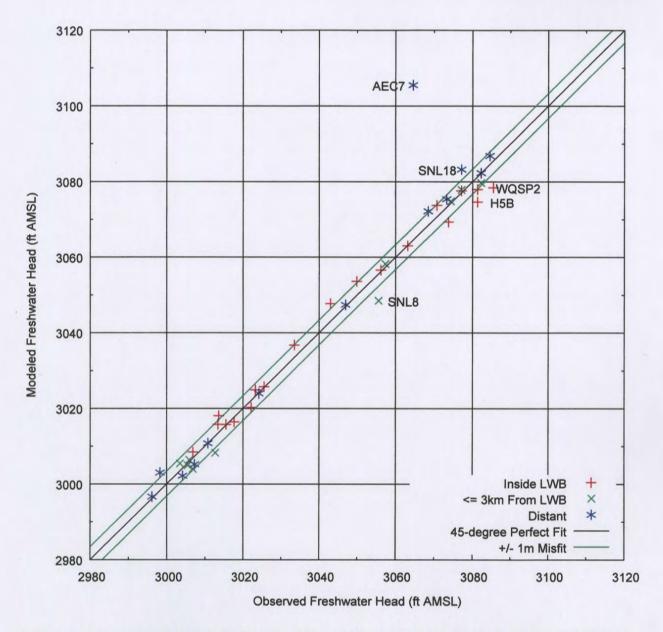


Figure 4. Measured vs. modeled scatter plot for PEST-calibrated MODFLOW-2000 generated heads and June 2009 observed freshwater heads

The central diagonal line in Figure 4 represents a perfect model fit (1:1 or 45-degree slope); the two lines on either side of this represent a 1-m misfit above or below the perfect fit. Wells more than 1.5 m from the 1:1 line are labeled. AEC-7 has a large misfit (12.5 m), for two reasons. First, this well has historically had an anomalously low freshwater head elevation, lower than wells around it in all directions. Secondly, it did not have a May 2007 observation (due to ongoing well reconfiguration activities) and therefore was not included as a calibration target in the PA MODFLOW model calibration. The ensemble-average T, A, and R fields used here were not calibrated to accommodate this

observation. This well is situated in a low-transmissivity region, and near the constant-head boundary associated with the halite margin, therefore PEST will not be able to improve this fit solely through adjustment of the boundary conditions indicated with red in Figure 1.

The R<sup>2</sup> value for the best-fit line through the measured vs. modeled data inside the WIPP LWB only is 0.982 (computed in Excel) and the slope of this best-fit line is 1.000. The R<sup>2</sup> value for a best-fit line through only the data from the intermediate zone is 0.993, with a slope of 1.000. The R<sup>2</sup> value for the best-fit line through the distant wells only is 0.920, with a slope of 1.001. The R<sup>2</sup> for the best-fit line through all wells together is 0.952, with a slope of 1.000.

Figure 5 and Figure 6 show the distribution of errors resulting from the PEST-adjusted fit to observed data. The distribution in Figure 5 is roughly symmetric about 0, indicating there is not a strong bias.

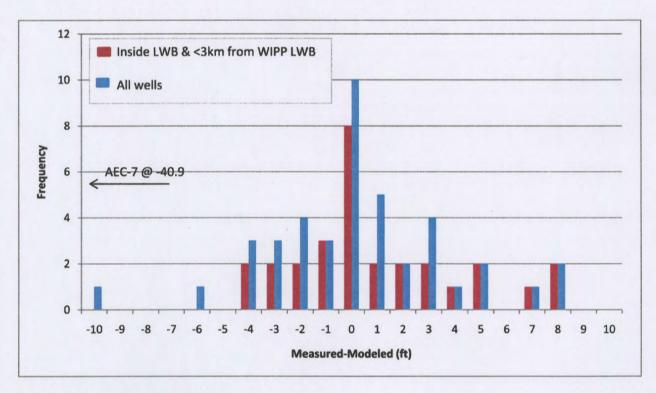


Figure 5. Histogram of Measured-Modeled errors

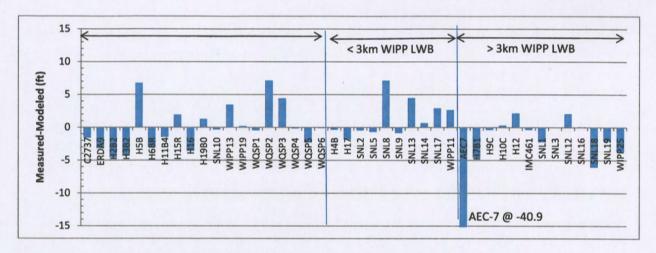


Figure 6. Measured-Modeled errors for each well with an observed September 2008 freshwater head

Aside from AEC-7, and to a lesser degree some other distant wells whose modeled values do not greatly impact the contours shown in Figure 2, the model fit to the June 2009 observations is very good. The ensemble-average model captures the average Culebra behavior, while the PEST calibration improved the model fit to the specific June 2009 observations.

#### 4 References

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#### **5** Run Control Narrative

This section is a narrative describing the calculation process mentioned in the text, which produced the figures given there.

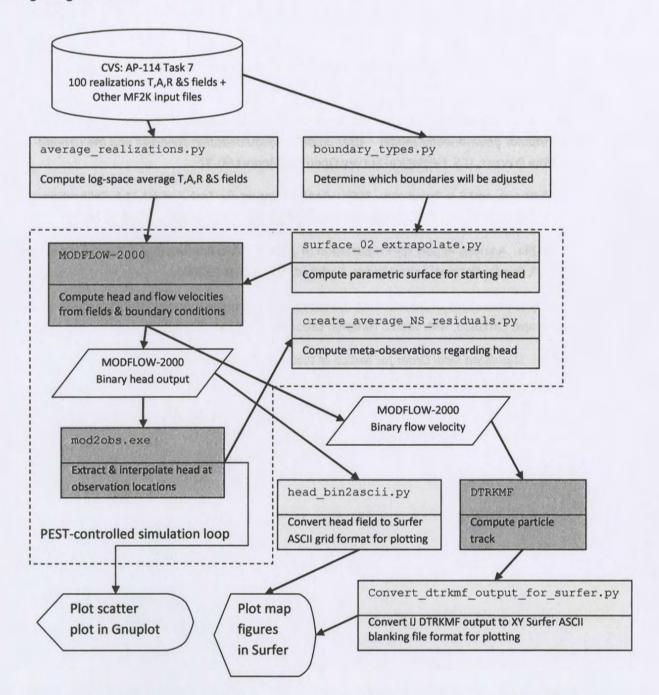


Figure 7. Process flowchart; dark gray indicates qualified programs, light gray are scripts written for this analysis

Figure 7 gives an overview of the driver script checkout\_average\_run\_modflow.sh (§A-4.1);

this script first exports the 4 parameter fields (transmissivity (T), anisotropy (A), recharge (R), and storativity (S)) from CVS for each of the 100 realizations of MODFLOW, listed in the file keepers (see lines 17-26 of script). Some of the realizations are inside the Update or Update2 subdirectories in CVS, which complicates the directory structure. An equivalent list keepers\_short is made from keepers, and the directories are moved to match the flat directory structure (lines 31-53). At this point, the directory structure has been modified but the MODFLOW input files checked out from CVS are unchanged.

The Python script average\_realizations.py (§A-4.2) is called, which first reads in the keepers\_short list, then reads in each of the 400 input files and computes the arithmetic average of the base-10 logarithm of the value at each cell across the 100 realizations. The 400 input files are saved as a flattened 2D matrix, in row-major order. The exponentiated result is saved in 4 parameter fields, each with the extension .avg instead of .mod. A single value from each file, corresponding to either the cell in the southeast corner of the domain (input file row 87188 = model row 307, model column 284 for K and A) or on the west edge of the domain (input file row 45157 = model row 161, model column 1 for R and S) is saved in the text file parameter\_representative\_values.txt to allow checking the calculation in Excel, comparing the results to the value given at the same row of the .avg file. The value in the right column of Table 3 can be found by taking the geometric average of the values in the text file, which are the values from the indicated line of each of the 100 realizations.

Table 3. Averaged values for representative model cells

Field	Input file row	Model row	Model column	Geometric average
K	87188	307	284	9.2583577E-09
Α	87188	307	284	9.6317478E-01
R	45157	161	1	1.4970689E-19
S	45157	161	1	4.0388352E-03

Figure 8 shows plots of the average log10 parameters, which compare with similar figures in Hart et al. (2009); inactive regions <1.0E-15 were reset to 1.0 to improve the plotted color scale. The rest of the calculations are done with these averaged fields.

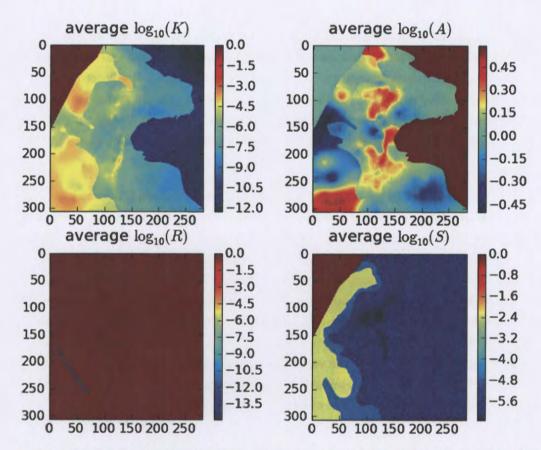


Figure 8. Plots of base-10 logarithms of average parameter fields; rows and columns are labeled on edges of figures.

Next, a subdirectory is created, and the averaged MODFLOW model is run without any modifications by PEST. Subsequently, another directory will be created where PEST will be run to improve the fit of the model to observed heads at well locations.

The next portion of the driving script <code>checkout\_average\_run\_modflow.sh</code> links copies of the input files needed to run MODFLOW-2000 and DTRKMF into the <code>original\_average</code> run directory. Then MODFLOW-2000 is run with the name file <code>mf2k\_head.nam</code>, producing binary head (<code>modeled\_head.bin</code>) and binary cell-by-cell flow budget (<code>modeled\_flow.bud</code>) files, as well as a text listing file (<code>modeled\_head.lst</code>). DTRKMF is then run with the input files <code>dtrkmf.in</code> and <code>wippctrl.inp</code>, which utilizes the cell-by-cell budget file written by MODFLOW to generate a particle track output file, <code>dtrk.out</code>. The input file <code>wippctrl.inp</code> specifies the starting location of the particle in DTRKMF face-centered cell coordinates, the porosity of the aquifer (here 16%), and the coordinates of the corners of the WIPP LWB, since the calculation stops when the particle reaches the LWB.

The Python script head\_bin2ascii.py (§A-4.7) converts the MODFLOW binary head file, which includes the steady-state head at every element in the flow model domain (307 rows × 284 columns) into a Surfer ASCII grid file format. This file is simply contoured in Surfer, no interpolation or gridding is needed. The Python script convert\_dtrkmf\_output\_for\_surfer.py (§A-4.9) reads the

DTRKMF output file dtrk.out and does two things. First it converts the row, column format of this output file to an X,Y format suitable for plotting, and second it converts the effective thickness of the Culebra from 7.75m to 4m. The following table shows the first 10 lines of the dtrk.out and the corresponding output of the Python script dtrk\_output\_original\_average.bln. The first three columns of dtrk.out (top half of Table 4) after the header are cumulative time (red), column (blue), and row (green). The three columns in the blanking file (second half of Table 4) after the header are UTM NAD27 X (blue), UTM NAD27 Y (green), and adjusted cumulative time (red, which is faster faster than the original cumulative travel time by the factor 7.75/4=1.9375). The conversion from row, column to X, Y is

```
X = 601700.0 + 100.0 * column

Y = 3597100.0 - 100.0 * row
```

since the I,J origin is the northwest corner of the model domain (601700,3597100), while the X,Y origin is the southwest corner of the domain. The blanking file is plotted directly in Surfer, since it now has the same coordinates as the ASCII head file.

Table 4. Comparison of first 10 lines of DTRKMF output and converted Surfer blanking file for original average

```
0.00000000E+00 118.79 150.21 1.18790000E+04 1.50210000E+04 0.00000000E+00 1.85168267E-01 1.59999996E-01 1.00000000E+00
  5.53946616E+01 118.86 150.29 1.18859872E+04 1.50285080E+04 1.02562574E+01 1.85130032E-01 1.59999996E-01 1.00000000E+00 1.10789323E+02 118.93 150.36 1.18929942E+04 1.50359947E+04 2.05104788E+01 1.85094756E-01 1.59999996E-01 1.00000000E+00
                        119.00 150.43 1.19000000E+04 1.50434379E+04 3.07321029E+01 1.85062532E-01 1.59999996E-01
  3.27990509E+02
                        119.21 150.62 1.19206651E+04 1.50624751E+04 5.88294962E+01 1.73534671E-01 1.59999996E-01 119.42 150.81 1.19415109E+04 1.50813473E+04 8.69490492E+01 1.73684593E-01 1.59999996E-01
                                                                                                                                                      1.00000000E+00
  4.89963060E+02
                                                                                                                                                      1.00000000E+00
                        119.62 151.00 1.19624759E+04 1.51000000E+04 1.15010608E+02 1.73860152E-01 1.59999996E-01 1.00000000E+00 119.75 151.10 1.19749757E+04 1.51102419E+04 1.31170520E+02 1.81333000E-01 1.59999996E-01 1.00000000E+00
   6.51450155E+02
  7.40581455E+02
                         119.87 151.20 1.19874963E+04 1.51204665E+04 1.47335525E+02 1.81390626E-01 1.59999996E-01 1.00000000E+00
613579.0,3582079.0,0.00000000e+00
613586.0,3582071.0,2.85907931e+01613593.0,3582064.0,5.71815861e+01
613600.0,3582057.0,8.56866885e+01
613621.0,3582038.0,1.69285424e+02
613642.0,3582019.0,2.52884160e+02
613662.0,3582000.0,3.36232338e+02
613675.0,3581990.0,3.82235590e+02
613687.0,3581980.0,4.28238841e+02
```

The PEST utility script mod2obs.exe is run to extract and interpolate the model-predicted heads at observation locations. The input files for mod2obs.exe were taken from AP-114 Task 7 in CVS. The observed head file has the wells and observed heads from June 2009, but is otherwise the same as that used in the model calibration in AP-114. The Python script

merge\_observed\_modeled\_heads.py (§A-4.9) simply puts the results from mod2obs.exe and the original observed heads in a single file together for plotting in Gnuplot and Excel.

A similar process to that described so far in this narrative is carried out in a new directory called pest\_02 (beginning line 146 of the driver script). The PEST calibration is carried out there, to keep it separate from the original\_average simulation. Now the Python script boundary\_types.py (§A-4.3) is also run, to create a new MODFLOW IBOUND array, where the two different types of boundary conditions are differentiated. This Python script uses the MODFLOW IBOUND array (init\_bnds\_orig.inf first ½ of Table 5) and the initial head array (init\_head\_orig.mod

middle ½ of Table 5) as inputs, and writes a new MODFLOW IBOUND array (init\_bnds.inf bottom ½ of Table 5) with constant-head nodes indicated in red in Figure 1 marked as -2 and other constant-head nodes remaining as -1 as output. The script differentiates between these two types of boundary conditions by checking if the starting head is <1000m. Starting heads >1000m are associated with the constant-head areas to the east of the halite margins (lighter gray areas in Figure 1).

Table 5. Input IBOUND, starting head, and output IBOUND array data corresponding to first row of MODFLOW model

0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0
	0 0 0 0 0 0 0 0 0 0 0 0
	0 0 0 0 0 0 0 0 0 0 0 0 -1
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1	
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	
943 943 943 943 943 943 943 943 943 943	T RET TO THE TOTAL
943 944 944 944 944 944 944 944 944 944	
944 944 944 944 944 944 944 944 944 944	
944 944 944 944 944 944 944 944 944 944	
944 944 944 944 944 944 944 944 944 944	
1085 1082 1081 1080 1079 1078 1078 1077 1077 1077 1077 1077	
1083 1084 1086 1086 1088 1090 1092 1095 1096 1098 1099 1099	
1104 1104 1104 1104 1104 1104 1105 1105	
	8 1119 1120 1121 1122 1123 1124 1125
1126 1127 1127 1129 1129 1130 1131 1132 1132 1133 1133 1133	
	4 1144 1144 1145 1145 1146 1147 1147
	8 1149 1150 1149 1149 1148 1149 1149
1151 1151 1151 1150 1152 1153 1154 1155	
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0
	0 0 0 0 0 0 0 0 0 0 0 0 -2
-2 -2 -2 -2 -2 -2 -2 -2 -2 -2 -2 -2 -2 -	2 -2 -2 -2 -2 -2 -2 -2 -2 -2 -2 -2
-2 -2 -2 -2 -2 -2 -2 -2 -2 -2 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1	1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1
-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -	1 -1 -1 -1 -1 -1

Table 5 shows the data corresponding to the northernmost row of the MODFLOW model domain (284 entries long) for the two input files and one output file. In the top IBOUND array, the values are either 0 or -1, indicating either inactive (the region northwest of the no-flow area shown in dark gray in Figure 1) or constant head (both red and light gray cells in Figure 1). The first 284 values from the initial head file (reformatted from scientific notation to integers to facilitate printing) show a jump from approximately 944 (in blue) to >1000 (in red). These same cells are colored in the output, showing how the initial head value is used to distinguish between the two types of constant-head boundaries. MODFLOW treats any cells as constant head which have an IBOUND entry < 0, so both -2 and -1 are the same to MODFLOW, but allow distinguishing between them in the Python script which extrapolates the heads to the boundaries.

The required PEST input files are created by the Python script <code>create\_pest\_02\_input.py</code> (§A-4.4). This script writes 1) the PEST instruction file (modeled\_head.ins), which shows PEST how to extract the model-predicted heads from the mod2obs.exe output; 2) the PEST template file

(surface\_par\_params.ptf), which shows PEST how to write the input file for the surface extrapolation script; 3) the PEST parameter file (surface\_par\_params.par), which lists the starting parameter values to use when checking the PEST input; 4) the PEST control file (bc\_adjust\_2009ASER.pst), which has PEST-related parameters, definitions of extrapolation surface parameters, and the observations and weights that PEST is adjusting the model inputs to fit. The observed heads are read as an input file in the PEST borehole sample file format (meas\_head\_2009ASER.smp), and the weights are read in from the input file (obs\_loc\_2009ASER.dat).

PEST runs the "forward model" many times, adjusting inputs and reading the resulting outputs using the instruction and template files created above. The forward model actually consists of a Bash shell script (run\_02\_model) that simply calls a pre-processing Python script surface\_02\_extrapolate.py (§A-4.5), the MODFLOW-2000 executable, the Python script create\_average\_NS\_residuals.py, and the PEST utility mod2obs.exe as a post-processing

create\_average\_NS\_residuals.py, and the PEST utility mod2obs.exe as a post-processing step. The script redirects the output of each step to /dev/null to minimize screen output while running PEST, since PEST will run the forward model many dozens of times.

The Python script <code>create\_average\_NS\_residuals.py</code> takes the output from the PEST utility <code>mod2obs.exe</code> and creates a meta-observation that consists of the average residual between measured and model-prediction, only averaged across the northern or southern WIPP wells (the wells in the center of the WIPP site are not included in either group). This was done to minimize cancelation of the errors north (where the model tended to underestimate heads) and south (where the model tended to overestimate heads) of the WIPP. The results of this script are read directly by PEST and incorporated as four additional observations (mean and median errors, both north and south of WIPP).

The pre-processing Python script  $surface_02_extrapolate.py$  reads the new IBOUND array created in a previous step (with -2 now indicating which constant-head boundaries should be modified), the initial head file used in AP-114 Task 7 (init\_head\_orig.mod), two files listing the relative X and Y coordinates of the model cells ( $rel_{x,y}_{coord.dat}$ ), and an input file listing the coefficients of the parametric equation used to define the initial head surface. This script then cycles over the elements in the domain, writing the original starting head value if the IBOUND value is -1 or 0, and writing the value corresponding to the parametric equation if the IBOUND value is -2 or 1. Using the parameters corresponding to those used in AP-114 Task 7, the output starting head file should be identical to that used in AP-114 Task 7.

After PEST has converged to the optimum solution for the given observed heads and weights, it runs the forward model one more time with the optimum parameters. The post-processing Python scripts for creating the Surfer ASCII grid file and Surfer blanking file from the MODFLOW and DTRKMF output are run and the results are plotted in Surfer. The figures in State Plane coordinates are converted from UTM using the US Army Corps of Engineers CorpsCon6 conversion software.

#### A-1 Input Files

input file name	file type	description
average_realizations.py	Python script	average 100 realizations
boundary_types.py	Python script	distinguish different BC types
checkout_average_run_modflow.sh	Bash script	main routine: checkout files, run MODFLOW and PEST, call Python scripts
convert_dtrkmf_output_for_surfer.py	Python script	convert DTRKMF IJ output to Surfer X,Y blanking format
create_pest_02_input.py	Python script	create PEST input files from observed data
dtrkmf.in	input listing	responses to DTRKMF prompts
head_bin2ascii.py	Python script	convert MODFLOW binary output to Surfer ASCII grid format
keepers	input	listing of 100 realizations from CVS
meas_head_2008ASER.smp	:	observed June 2009 heads
meas_nead_2000ASER.Smp	input	in mod2obs.exe bore sample file format
merge_observed_modeled_heads.py	Python script	paste observed head and model-generated heads into one file
mod2obs_files.dat	file listing	files needed to run mod2obs.exe
mod2obs_head.in	input listing	responses to mod2obs.exe prompts
modflow_files.dat	file listing	files needed to run MODFLOW
obs_loc_2008ASER.dat	input	listing of wells and geographic groupings
pest_02_files.dat	file listing	files needed to run PEST
rel_x_coord.dat	input	relative coordinate $1 \le x \le 1$
rel_y_coord.dat	input	relative coordinate $1 \le y \le 1$
run_02_model	Bash script	PEST model: execute MODFLOW and do pre- and post-processing
settings.fig	input	mod2obs.exe input file
spec_domain.spc	input	mod2obs.exe input file
spec_wells.crd	input	mod2obs.exe input file
surface_02_extrapolate.py	Python script	compute starting head from parameter and coordinate inputs
wippctrl.inp	input	DTRKMF input file
create_average_NS_residuals.py	Python script	create meta-observations of northern and southern average heads

Table A-1: Input Files

#### A-2 Output Files

output file name	file type	description
ASER_boundary_StPl.bln	Surfer	coordinates defining contouring area
	blanking file	in state plane coordinates
ASER_area_only_state_plane.srf	Surfer Plot file	plot of local contours
ASER_area_only_state_plane.emf	enhanced metafile	plot of local contours
regional_plot_state_plane.srf	Surfer Plot file	plot of regional contours
regional_plot_state_plane.emf	enhanced metafile	plot of regional contours
	Surfer	coords defining particle track: output from
dtrk_output_pest_02_StPl.bln	blanking file	convert_dtrkmf_output_for_surfer.py
		in state plane (converted via CorpsCon6)
modeled_head_pest_02_StPl.grd	Surfer grid file model-generated heads: output from head_bin2ascii.py	model-generated heads:
modeled_nead_pest_02_5till.grd		1
modeled_vs_observed_head_pest02.xlsx	Excel spreadsheet	modeled_vs_observed_head_pest_02.txt
modered_vs_observed_nead_pesto2.xisx		plotted for histograms & regression $\mathbb{R}^2$ values
plot_scatter_plots.gnu	gnuplot input	<pre>input for plotting scatter_pest_02_feet.emf</pre>
scatter_pest_02_feet.emf	enhanced metafile	output from gnuplot
wipp_boundary_StPl.bln	Surfer	coordinates defining WIPP LWB
wipp_boundary_buri.bin	blanking file	in state plane coordinates
well_data_with_names_and_observed.dat	coords/names	well coordinates and names for plotting

Table A-2: Output Files

#### A-3 Directory Listings

```
C:\>dir input
Volume in drive C is DriveC
 Volume Serial Number is 542A-10F7
Directory of C:\input
05/06/2010 12:48 PM
                      <DIR>
05/06/2010 12:48 PM
                      <DIR>
08/28/2009 03:06 PM
                               2,057 average_realizations.py
08/25/2009 01:00 PM
                              2,088 boundary_types.py
08/25/2009 12:58 PM
                             6,650 checkout_average_run_modflow.sh
08/25/2009 01:04 PM
                                 630 convert_dtrkmf_output_for_surfer.py
                             1,801 create_average_NS_residuals.py
04/21/2010 05:13 PM
                             2,980 create_pest_02_input.py
04/21/2010 05:47 PM
04/02/2010 02:37 PM
                                  48 dtrkmf.in
08/25/2009 01:03 PM
                             3,862 head_bin2ascii.py
04/02/2010 02:37 PM
                              1,091 keepers
05/03/2010 03:11 PM
                                 968 merge_observed_modeled_heads.py
04/02/2010 02:37 PM
                                 76 mod2obs_files.dat
04/02/2010 04:19 PM
                                 138 mod2obs_head.in
04/02/2010 02:37 PM
                                 372 modflow_files.dat
04/02/2010 02:33 PM
                                 400 obs_loc_2009ASER.dat
04/21/2010 05:31 PM
                                 215 pest_02_files.dat
04/02/2010 02:37 PM 2,397,670 rel_x_coord.dat
04/02/2010 02:37 PM
                         2,397,528 rel_y_coord.dat
04/21/2010 05:31 PM
                                 389 run_02_model
04/02/2010 02:37 PM
                                 26 settings.fig
04/02/2010 02:37 PM
                                 47 spec_domain.spc
04/02/2010 02:55 PM
                              1,705 spec_wells.crd
08/25/2009 01:02 PM
                               2,463 surface_02_extrapolate.py
04/02/2010 02:37 PM
                                 506 wippctrl.inp
             23 File(s) 4,823,710 bytes
              2 Dir(s) 149,809,336,320 bytes free
```

```
C:\>dir output
Volume in drive C is DriveC
Volume Serial Number is 542A-10F7
Directory of C:\output
05/06/2010 01:01 PM
                       <DIR>
05/06/2010 01:01 PM
                        <DIR>
05/04/2010 04:32 PM
                              217,848 ASER_area_only_state_plane.emf
05/04/2010 04:30 PM
                              938,326 ASER_area_only_state_plane.srf
05/04/2010 04:08 PM
                                  120 ASER_boundary_StPl.bln
05/04/2010 04:22 PM
                                5,059 dtrk_output_pest_02_StPl.bln
05/04/2010 03:50 PM
                              697,604 modeled_head_XYZ_StPl.grd
05/04/2010 01:32 PM
                                2,099 modeled_vs_observed_head_pest_02.txt
05/06/2010 12:51 PM
                               34,444 modeled_vs_observed_head_pest_02.xlsx
05/03/2010 03:44 PM
                                2,203 plot_scatter_plots.gnu
05/05/2010 07:23 AM
                              217,104 regional_plot_state_plane.emf
05/05/2010 07:22 AM
                              915,546 regional_plot_state_plane.srf
05/03/2010 03:44 PM
                               33,352 scatter_pest_02_feet.emf
05/04/2010 04:04 PM
                                  120 wipp_boundary_StPl.bln
             12 File(s)
                             3,063,825 bytes
              2 Dir(s) 149,808,885,760 bytes free
```

#### A-4.1 Bash shell script checkout\_average\_run\_modflow.sh

```
\#!/bin/bash
2
3
  #
     this script makes the following directory substructure
4
  #
  #
                        - Outputs
                                   (calibrated\ parameter\ fields-INPUTS)
5
      current_{-}dir
  #
                                    (other\ modflow\ files-INPUTS)
6
                        -Inputs
   #
                         original\_average (foward sim using average fields)
7
                                    (MODFLOW and DTRKMF binaries)
8
                          pest_-0?
                                   (pest-adjusted results)
9
10
11
   echo " checking out T fields"
12
   echo " ^^^^
13
   \# these will checkout the calibrated parameter-field data into subdirectories
15
   \# checkout things that are different for each of the 100 realiztaions
16
   for d in 'cat keepers'
17
18
     cvs -d /nfs/data/CVSLIB/Tfields checkout Outputs/${d}/modeled_{K,A,R,S}_field.mod
19
   done
20
21
   \# checkout MODFLOW input files that are constant for across all realizations
22
   cvs -d /nfs/data/CVSLIB/Tfields checkout Inputs/data/elev_{top, bot}.mod
23
   cvs -d /nfs/data/CVSLIB/Tfields checkout Inputs/data/init_{bnds.inf,head.mod}
24
   cvs -d /nfs/data/CVSLIB/Tfields checkout Inputs/modflow/mf2k_culebra.{lmg,lpf}
25
   cvs -d /nfs/data/CVSLIB/Tfields checkout Inputs/modflow/mf2k_head.{ba6,nam,oc,dis,rch}
26
27
   # modify the path of "updated" T-fields, so they are all at the
   \# same level in the directory structure (simplifying scripts elsewhere)
30
      -a keepers_short
31
32
       rm keepers_short
33
34
   touch keepers_short
35
36
   for d in 'cat keepers'
37
   do
38
     bn='basename ${d}'
39
     \# \ test \ whether \ it \ is \ a \ compount \ path
40
     if [ ${d} != ${bn} ]
41
         then
42
         dn='dirname ${d}'
43
         mv ./Outputs/${d} ./Outputs/
45
         # put an empty file in the directory to indicate
46
         \# what the directory was previously named
47
         touch ./Outputs/{bn}/{dn}
48
49
50
     \# create a keepers list without directories
51
     echo ${bn} >> keepers_short
52
53
   echo " .....
          perform averaging across all realizations "
57
58
   python average_realizations.py
59
60
   # checkout MODFLOW / DTRKMF executables
```

```
cvs -d /nfs/data/CVSLIB/MODFLOW2K checkout bin/mf2k/mf2k_1.6.release
62
   cvs -d /nfs/data/CVSLIB/MODFLOW2K checkout bin/dtrkmf/dtrkmf_v0100
63
64
   # check out pest and obs2mod binaries
65
   cd bin
66
   cvs -d /nfs/data/CVSLIB/PEST checkout Builds/Linux/pest.exe
67
   cvs -d /nfs/data/CVSLIB/PEST checkout Builds/Linux/mod2obs.exe
70
   echo " setup copies of files constant between all realizations
72
73
   \# directory for putting original base-case results in
75
   od=original_average
76
77
   if [ -d ${od} ]
78
   then
79
       echo ${od}" directory exists: removing and re-creating"
80
       rm - rf \$ \{od\}
81
   fi
82
83
   mkdir ${od}
   cd ${od}
   echo 'pwd'
86
   # link to unchanged input files
88
   for file in 'cat .. / modflow_files.dat'
89
90
     ln - sf \$\{file\}.
91
   done
92
93
   \# link to averaged files computed in previous step
94
   for f in \{A,R,K,S\}
95
   \mathbf{do}
96
     ln - sf ... / modeled_{f}_{f}_{field.avg} ... / modeled_{f}_{f}_{field.mod}
97
   done
   ln -sf elev_top.mod fort.33
100
   \ln -\text{sf elev\_bot.mod fort.}34
101
102
        103
   echo " run original MODFLOW and DTRKMF and export results for plotting"
104
105
106
   # run MODFLOW, producing average head and CCF
107
   ../bin/mf2k/mf2k_1.6.release mf2k_head.nam
108
109
   # run DTRKMF, producing particle track (from ccf)
110
   ../bin/dtrkmf/dtrkmf_v0100 <dtrkmf.in
112
   \# convert binary MODFLOW head output to Surfer ascii grid file format
113
   ln -sf ../head_bin2ascii.py
114
   python head_bin2ascii.py
115
   mv modeled_head_asciihed.grd modeled_head_${od}.grd
116
117
   \# convert DTRKMF output from cells to X,Y and
118
   \# save in Surfer blanking file format
119
   ln -sf ../convert_dtrkmf_output_for_surfer.py .
120
   python convert_dtrkmf_output_for_surfer.py
   mv dtrk_output.bln dtrk_output_${od}.bln
122
   # extract head results at well locations and merge with observed
124
   \# head file for easy scatter plotting in Excel (tab delimited)
```

```
for file in 'cat ../mod2obs_files.dat'
126
127
      \ln -sf \$\{file\}.
128
   done
129
130
   ln - sf ... / meas\_head\_2008ASER.smp.
131
   ln - sf ... / obs\_loc\_2008ASER.dat.
132
    ../bin/Builds/Linux/mod2obs.exe <mod2obs_head.in
   In -sf ../merge_observed_modeled_heads.py
   python merge_observed_modeled_heads.py
   mv both_heads.smp modeled_vs_observed_head_${od}.txt
136
137
   # go back down into root directory
138
   cd ...
139
   echo 'pwd'
140
141
   echo "
142
   echo " setup and run PEST to optimize parametric surface to set BC "
143
144
145
   for p in pest_02
146
147
   do
      if [ -d ${p} ]
149
          then
150
          echo ${p}" directory exists: removing and re-creating"
151
          rm - rf \$\{p\}
152
      fi
153
154
      mkdir ${p}
155
      cd ${p}
156
      echo 'pwd'
157
158
      \#\ link\ to\ unchanged\ input\ files
159
      for file in 'cat .. / modflow_files.dat'
160
161
        \ln -sf \$\{file\}.
162
163
      done
164
      \#\ link\ to\ averaged\ files\ computed\ in\ previous\ step
165
      for f in \{A,R,K,S\}
166
167
        ln - sf ... / modeled_{f}_{f}_{field.avg} ... / modeled_{f}_{f}_{field.mod}
168
      done
169
170
      \#\ link\ to\ mod2obs\ files\ (needed\ for\ pest)
171
      for file in 'cat .. / mod2obs_files.dat'
172
173
        \ln -sf \$\{file\}.
174
      done
175
176
177
      \# link to pest files
      for file in 'cat ../${p}_files.dat'
178
179
        \ln -s  ${file}.
180
      done
181
182
      \# rename 'original' versions of files to be modified by pest
183
     rm init_head.mod
184
      ln -sf ../Inputs/data/init_head.mod ./init_head_orig.mod
185
     rm init_bnds.inf
186
      ln -sf ../Inputs/data/init_bnds.inf ./init_bnds_orig.inf
187
      \# create new ibound array for easier modification during PEST
189
```

```
# optimization iterations
190
     python boundary_types.py
191
192
     # create the necessary input files from observations
193
     python create_${p}_input.py
194
195
     # run pest
196
      ../bin/Builds/Linux/pest.exe bc_adjust_2008ASER
     # last output files should be best run
     \# extract all the stuff from that output
     201
     \ln -sf elev_top.mod fort.33
203
     \ln -sf elev_bot.mod fort.34
204
205
      ../bin/dtrkmf/dtrkmf_v0100 <dtrkmf.in
206
207
     ln -sf ../head_bin2ascii.py .
208
     python head_bin2ascii.py
209
     mv modeled_head_asciihed.grd modeled_head_${p}.grd
210
211
     ln -sf ../convert_dtrkmf_output_for_surfer.py .
212
     python convert_dtrkmf_output_for_surfer.py
     mv dtrk_output.bln dtrk_output_${p}.bln
214
215
     for file in 'cat .. / mod2obs_files.dat'
216
217
       \ln -sf \$\{file\}.
218
219
220
      ../bin/Builds/Linux/mod2obs.exe <mod2obs_head.in
221
     ln -sf ../merge_observed_modeled_heads.py
222
     python merge_observed_modeled_heads.py
223
     mv both_heads.smp modeled_vs_observed_head_${p}.txt
224
     cd ...
   done
```

#### A-4.2 Python script average\_realizations.py

```
from math import log10, pow
   nrow = 307
3
   ncol = 284
   nel = nrow*ncol
   nfr = 100 \# number of fields (realizations)
               # number of field types
   debug = True \# set to True to get output described in RunControl narrative
9
10
11
   def floatload (filename):
        """Reads file (a list of strings, one per row) into a list of strings."""
12
        f = open(filename, 'r')
13
       m = [float(line.rstrip())] for line in f
14
       f.close()
15
       return m
16
17
   types = ['K', 'A', 'R', 'S']
18
19
   \# get list of 100 best calibrated fields
20
   flist = open('keepers_short','r')
21
   runs = flist.read().strip().split('\n')
22
   flist.close()
23
24
   # initialize to help speed lists up a bit
25
26
   \# nfr (100) realizations of each
   fields = []
27
   for i in xrange(nft):
28
        fields.append([None]*nfr)
29
        for i in xrange(nfr):
30
            # each realization being nel (87188) elements
31
            fields[-1][i] = [None]*nel
32
33
   # read in all realizations
34
   print 'reading ...'
35
   for i, run in enumerate (runs):
        print i, run
        for j, t in enumerate (types):
            fields[j][i][0:nel] = floatload('Outputs/'+run+'/modeled_'+t+'_field.mod')
40
   \# save file with one cell from each realization for checking in Excel
41
   if debug:
42
        print 'writing debugging output for checking'
43
        \mathrm{fd} = \mathrm{open}(\, '\mathtt{parameter\_representative\_values.txt'}\, , '\mathtt{w'})
44
        fd.write('%s %18s %18s %18s %18s\n'%
45
                   'rzn', types [0], types [1], types [2], types [3]))
46
        for i, run in enumerate (runs):
47
            {
m fd.write} ( '%s %.14e %.14e %.14e %.14e\n' \%
48
                       (\text{run}, \text{fields}[0][i][-1], \text{fields}[1][i][-1],
49
                        fields [2][i][159*284], fields [3][i][159*284]))
50
        fd.close()
51
52
53
   # open up files for writing
   fh = []
54
   for t in types:
55
       fh.append(open('modeled_'+ t +'_field.avg','w'))
56
57
   # transpose fields to allow slicing across realizations, rather than across cells
58
   for j in range (len (types)):
59
        fields[j] = zip(*(fields[j]))
60
   print 'writing ...'
   # do averaging across 100 realizations
```

```
for i in xrange(nel):
    if i%10000 == 0:
        print i
for h,d in zip(fh, fields):
        h.write('%18.11e\n' % pow(10.0,sum(map(log10,d[i]))/nfr))
for h in fh:
        h.close()
```

```
from itertools import chain
                  # number columns in model grid
3
   ny = 307
                  # number rows
4
   nel = nx*ny
   def intload (filename):
7
       """Reads file (a 2D integer array) as a list of lists.
       Outer list is rows, inner lists are columns."""
9
       f = open(filename, 'r')
10
       m = [[int(v) for v in line.rstrip().split()] for line in f]
11
12
       f.close()
       return m
13
14
   def intsave (filename, m):
15
       """Writes file as a list of lists as a 2D integer array, format '%3i'.
16
       Outer list is rows, inner lists are columns."""
17
       f = open(filename, 'w')
18
       for row in m:
19
            f.write(' '.join(['%2i' % col for col in row]) + '\n')
20
       f.close()
21
22
   def floatload (filename):
23
       """Reads file (a list of real numbers, one number each row)
24
       into a list of floats."""
25
26
       f = open(filename, 'r')
       \mathbf{m} = [\text{float}(\text{line.rstrip}()) \text{ for line in } f]
27
       f.close()
28
       return m
29
30
   def reshapev2m(v):
31
       """Reshape a vector that was previously reshaped in C-major order
32
       from a matrix, back into a matrix (here a list of lists)."""
33
       m = [None] * ny
34
       for i, (lo, hi) in enumerate (zip (xrange (0, \text{nel}-\text{nx}+1, \text{nx}), xrange (\text{nx}, \text{nel}+1, \text{nx})):
           m[i] = v[lo:hi]
       return m
39
   40
   \# read in original MODFLOW IBOUND array (only 0,1, and -1)
41
   ibound = intload('init_bnds_orig.inf')
42
43
   # read in initial heads
44
   h = reshapev2m(floatload('init_head_orig.mod'))
45
46
   # discriminate between two types of constant head boundaries
47
   \# -1) CH, where value > 1000 (area east of halite margin)
   \# -2) CH, where value < 1000 (single row/column of cells along domain edge
49
50
   for i, row in enumerate (ibound):
51
       for j, val in enumerate (row):
52
53
            \# is this constant head and is starting head less than 1000m ?
            if ibound [i][j] == -1 and h[i][j] < 1000.0:
54
                ibound [i][j] = -2
55
56
   \# save new IBOUND array that allows easy discrimination between types
57
   \# in python script during PEST optimization runs, and is still handled
   \# the same by MODFLOW since all ibound values < 0 are constant head.
   intsave('init_bnds.inf',ibound)
```

```
prefix = '2009ASER'
  ## pest instruction file reads output from mod2obs
  fin = open('meas_head_%s.smp' % prefix,'r')
  # each well is a [name, head] pair
   wells = [[line.split()]0], line.split()[3]] for line in fin
   fin.close()
   fout = open('modeled_head.ins','w')
11
   fout.write('pif @\n')
12
   for i, well in enumerate (wells):
13
          fout.write("11 [%s]39:46\n" % well[0])
14
   fout.close()
15
16
  # exponential surface used to set initial head everywhere
17
  # except east of the halite margins, where the land surface is used.
18
  # initial guesses come from AP-114 Task report
  params = [928.0, 8.0, 1.2, 1.0, 1.0, -1.0, 0.5]
   pnames = ['a',
                   'b', 'c', 'd', 'e', 'f', 'exp']
  fout = open('avg_NS_res.ins','w')
  fout.write("""pif @
  11 [medianN]1:16
  11 [medianS]1:16
  11 [meanN]1:16
  11 [meanS]1:16
28
  """)
29
   fout.close()
30
31
32
  33
  ## pest template file
  ftmp = open('surface_par_params.ptf','w')
   ftmp.write('ptf @\n')
   for n in pnames:
                           %s
                                     @\n, % n)
          ftmp.write('0
   ftmp.close()
40
41
  42
  ## pest parameter file
43
44
   fpar = open('surface_par_params.par','w')
45
   fpar.write('double point\n')
46
   for n,p in zip (pnames, params):
47
      fpar.write('%s %.2f 1.0 0.0\n' % (n,p))
48
49
   fpar.close()
50
51
  ## pest control file
54
  f = open('bc_adjust_%s.pst' % prefix,'w')
55
56
  f. write ("""pcf
57
  * control data
58
  restart estimation
  %i %i 1 0 2
  1 2 double point 1 0 0
  5.0 2.0 0.4 0.001 10
  3.0 3.0 1.0E-3
```

```
0.1
   30 0.001 6 6 0.0001 4
65
   1 1 1
   * parameter groups
   bc relative 0.005 0.0001 switch 2.0 parabolic
   """ \% (len (params), len (wells)+4))
69
70
   f.write('* parameter data\n')
   for n,p in zip(pnames, params):
72
            if p > 0:
                     f.write('%s none relative %.3f %.3f %.3f
                                                                                       1\n'%
                                                                        bс
                                                                            1.0 0.0
                              (n, p, -2.0*p, 3.0*p))
75
            else:
76
                                                          %.3f %.3f
                     f.write('%s none relative %.3f
                                                                        bc
                                                                             1.0
                                                                                 0.0
                                                                                       1\n'%
77
                              (n, p, 3.0*p, -2.0*p))
78
79
   f.write("""* observation groups
80
   ss_head
81
   avg_head
82
   * observation data
83
84
85
   \#\#\ read\ in\ observation\ weighting\ group\ definitions
   fin = open('obs_loc_%s.dat' % prefix ,'r')
   location = [line.rstrip().split()] for line in fin
   fin.close()
89
90
   weights = []
91
92
   for l in location:
93
        # inside LWB
94
        if l = 0:
95
            weights.append (2.5)
96
        # near LWB
97
        if l = '1':
98
            weights.append(1.0)
99
       # distant to LWB
        if 1 = '2':
101
            weights append (0.4)
102
103
   for name, head, w in zip(zip(*wells)[0], zip(*wells)[1], weights):
104
        f.write('%s %s %.3f ss_head\n' % (name, head, w))
105
106
   \# there are 13 N observations in the average and 11 S, therefore
107
   # split the weight between the mean and median
108
   f.write("""medianN
                         0.0 13.0
                                    avg_head
109
   medianS
             0.0 13.0
                         avg_head
110
             0.0 11.0
   meanN
                         avg_head
111
             0.0 11.0
   meanS
                         avg_head
112
114
   f.write("""* model command line
115
   ./run_02_model
116
   * model input/output
117
   surface_par_params.ptf surface_par_params.in
118
   modeled_head.ins modeled_head.smp
119
   avg_NS_res.ins avg_NS_res.smp
120
   " " ii )
121
   f.close()
122
```

```
A-4.5 Python script surface_02_extrapolate.py

from itertools import chain
from math import sqrt

def matload(filename):
    """Reads file (a 2D string array) as
    Outer list is rows, inner lists are
```

```
2
4
       """Reads file (a 2D string array) as a list of lists.
5
       Outer list is rows, inner lists are columns."""
6
       f = open(filename, 'r')
       m = [line.rstrip().split() for line in f]
9
       f.close()
       return m
10
11
12
   def floatload (filename):
       """Reads file (a list of real numbers, one number each row)
13
       into a list of floats."""
14
       f = open(filename, 'r')
15
       m = [float(line.rstrip()) for line in f]
16
       f.close()
17
       return m
18
19
   def reshapem2v(m):
20
       """Reshapes a rectangular matrix into a vector in same fashion
21
       as numpy.reshape(), which is C-major order"""
22
       return list (chain (*m))
23
24
   \mathbf{def} \operatorname{sign}(\mathbf{x}):
25
       """ sign function"""
26
       if x < 0:
27
            return -1
28
       elif x>0:
29
           return +1
30
       else:
31
           return 0
32
33
   34
   # read in modified IBOUND array, with the cells to <math>modify set to -2
   ibound = reshapem2v(matload('init_bnds.inf'))
   h = floatload('init_head_orig.mod')
39
40
   # these are relative coordinates, -1 \le x, y < +1
41
   x = floatload('rel_x_coord.dat')
42
   y = floatload('rel_y_coord.dat')
43
44
   # unpack surface parameters (one per line)
45
   \# z = A + B*(y + D*sign(y)*sqrt(abs(y))) + C*(E*x**3 - F*x**2 - x)
46
47
   finput = open('surface_par_params.in','r')
48
49
       a,b,c,d,e,f,exp = [float(line.rstrip()) for line in finput]
50
   except ValueError:
51
       # python doesn't like 'D' in 1.2D-4 notation used by PEST sometimes.
52
53
       finput.seek(0)
       lines = [line.rstrip() for line in finput]
54
       for i in range (len (lines)):
55
            lines [i] = lines [i].replace('D', 'E')
56
       a,b,c,d,e,f,exp = [float(line) for line in lines]
57
58
   finput.close()
59
60
   \# file to output initial/boundary head for MODFLOW model
   fout = open('init_head.mod','w')
```

for i in xrange(len(ibound)):

Information Only

```
if ibound [i] = '-2' or ibound [i] = '1':
64
            \# apply surface to active cells (ibound=1) \rightarrow starting guess
65
            \# and non-geologic boundary conditions (ibound=-2) -\!\!> constant head
66
            \mathbf{if} \ y[i] == 0:
67
                fout.write('%.7e \n' % (a + c*(e*x[i]**3 + f*x[i]**2 - x[i])))
68
            else:
69
                fout.write('%.7e \n' % (a + b*(y[i] + d*sign(y[i])*abs(y[i])**exp) +
70
                                          c*(e*x[i]**3 + f*x[i]**2 - x[i]))
       else:
72
            # use land surface at constant head east of halite boundary
73
            # ibound=0 doesn't matter (inactive)
            fout.write('\%.7e\n' \% h[i])
75
   fout.close()
```

#### A-4.6 Python script create\_average\_NS\_residuals.py

```
# this python script computes some summary residuals
   # based on the concept of "north of WIPP" and "south of WIPP"
   # to get PEST to honor the areas outside the steep gradient
   \# across the site.
4
   \mathbf{def} median(x):
6
        """return median of a list of floats"""
       y = x :
       y.sort()
9
       ly = len(y)
10
11
        if 1y\%2 == 0:
12
            return (y[ly/2-1] + y[ly/2])/2.0
13
        else:
14
            return y[(ly-1)/2]
15
16
   north = ['H6bR', 'WQSP1', 'WIPP13', 'WQSP2', 'WIPP11', 'SNL2', 'SNL5',
17
             'WIPP25','SNL19','SNL3','SNL18','SNL1','H5b']
18
19
   south = ['SNL16','SNL13','H4b','H11b4','SNL14','H17','SNL17',
20
             'H12','H7b1','SNL12','H9c']
21
22
   north = [x.upper() for x in north]
23
   south = [x.upper() for x in south]
25
   # make a dictionary of wells with heads as values
26
   wells = \{\}
27
28
   # read in measured heads
29
   fhsmp = open('meas_head_2009ASER.smp','r')
30
   for line in fhsmp:
31
       name, j1, j2, meas = line.strip().split()
32
        wells [name.upper()] = {'meas':float(meas)}
33
   fhsmp.close()
34
   \# read in modeled heads
   fhmod = open('modeled_head.smp','r')
   for line in fhmod:
       name, j1, j2, mod = line.strip().split()
        wells [name.upper()]['mod'] = float (mod)
40
   fhmod.close()
41
42
   #for well in wells.keys():
43
        print well, wells [well]
44
45
   # compute residuals north and south of WIPP
46
   resN = []
47
   \#print , north ,
48
   for w in north:
49
       resN.append(wells[w]['meas'] - wells[w]['mod'])
50
        print \ w, wells [w] \ 'meas'], wells [w] \ 'mod'], wells [w] \ 'meas'] - wells [w] \ 'mod']
51
52
   \#print 'south'
53
   resS = []
54
   for w in south:
55
       resS.append(wells [w] ['meas'] - wells [w] ['mod'])
56
        print \ w, wells [w] \ 'meas'], wells [w] \ 'mod'], wells [w] \ 'meas'] - wells [w] \ 'mod']
57
58
   fhout = open('avg_NS_res.smp','w')
59
   fhout.write('%.7e \n' % median(resN))
   fhout.write('%.7e \n' % median(resS))
   fhout.write('%.7e \n' % (sum(resN)/len(resN),))
   fhout.write('%.7e \n' % (sum(resS)/len(resS))
```

#### A-4.7 Bash shell script run\_02\_model

```
\#!/bin/bash
  \#set - o xtrace
  #echo 'step 1: surface extrapolate'
  python surface_02_extrapolate.py
  # run modflow
  \#echo 'step 2: run modflow'
   ../bin/mf2k/mf2k_1.6.release mf2k_head.nam >/dev/null
10
  \# run mod2obs
  #echo 'step 3: extract observations'
13
   ../bin/Builds/Linux/mod2obs.exe < mod2obs_head.in >/dev/null
14
15
  \# create meta-observations of N vs. S
   python create_average_NS_residuals.py
```

```
import struct
   class FortranFile (file):
3
       """ modified from May 2007 Enthought-dev mailing list
4
       post by Neil Martinsen-Burrell"""
5
6
        \mathbf{def} = \mathbf{init} = (\mathbf{self}, \mathbf{fname}, \mathbf{mode} = \mathbf{r'r'}, \mathbf{buf} = 0):
            file.__init__(self, fname, mode, buf)
            self.ENDIAN = ' < ' \# little endian
            self.di = 4 # default integer (could be 8 on 64-bit)
10
        def readReals(self, prec='f'):
            """Read in an array of reals (default single precision)
13
            with error checking"""
14
            \# read header (length of record)
15
            1 = struct.unpack(self.ENDIAN+'i', self.read(self.di))[0]
16
            data_str = self.read(1)
17
            len_real = struct.calcsize(prec)
18
            if 1 % len_real != 0:
19
                raise IOError('Error reading array of reals from data file')
20
           num = 1/len_real
21
            reals = struct.unpack(self.ENDIAN+str(num)+prec,data_str)
22
            \# \ check \ footer
            if struct.unpack(self.ENDIAN+'i', self.read(self.di))[0] != 1:
                raise IOError('Error reading array of reals from data file')
26
            return list (reals)
        def readInts(self):
28
            """Read in an array of integers with error checking"""
29
            1 = struct.unpack('i', self.read(self.di))[0]
30
            data_str = self.read(1)
31
            len_int = struct.calcsize('i')
32
            if 1 % len_int != 0:
                raise IOError('Error reading array of integers from data file')
            num = 1/len_int
            ints = struct.unpack(str(num)+'i', data_str)
            if struct.unpack(self.ENDIAN+'i', self.read(self.di))[0] != 1:
                raise IOError('Error reading array of integers from data file')
            return list (ints)
40
        def readRecord (self):
41
            """Read a single fortran record (potentially mixed reals and ints)"""
42
            dat = self.read(self.di)
43
            if len(dat) == 0:
44
                raise IOError('Empy record header')
45
            l = struct.unpack(self.ENDIAN+'i', dat)[0]
46
            data_str = self.read(1)
47
            if len(data_str) != 1:
                raise IOError('Didn'' read enough data')
49
            check = self.read(self.di)
            if len(check) != 4:
                raise IOError('Didn''t read enough data')
            if struct.unpack(self.ENDIAN+'i',check)|0| != 1:
                raise IOError('Error reading record from data file')
54
            return data_str
55
56
   def reshapev2m (v, nx, ny):
57
        """Reshape a vector that was previously reshaped in C-major order
58
       from a matrix, back into a C-major order matrix (here a list of lists)."""
59
       m = [None]*ny
60
       n = nx*ny
61
       for i, (lo, hi) in enumerate (zip (xrange (0, n-nx+1, nx)), xrange (nx, n+1, nx))):
62
           m[i] = v[lo:hi]
```

```
return m
64
65
   def floatmatsave (filehandle, m):
66
        """Writes array to open filehandle, format '568%e12.5'.
67
        Outer list is rows, inner lists are columns."""
68
69
        for row in m:
70
            f.write(''.join([' \frac{12.5e}{m} col for col in row]) + '\n')
72
   # open file and set endian-ness
73
    ff = FortranFile('modeled_head.bin')
76
   # currently this assumes a single-layer MODFLOW model
77
   # (or at least only one layer of output)
78
   # format of MODFLOW header in binary layer array
79
   fmt = '<2i2f16s3i'
80
     little\ endian, 2 integers, 2 floats,
81
         16-character string (4 element array of 4-byte strings), 3 integers
82
83
   while True:
84
        \mathbf{try}:
85
            # read in header
            h = ff.readRecord()
        except IOError:
89
            # exit while loop
90
            break
91
92
        else:
93
            # unpack header
94
            kstp, kper, pertim, totim, text, ncol, nrow, ilay = struct.unpack(fmt, h)
95
96
            # print status/confirmation to terminal
97
            print kstp, kper, pertim, totim, text, ncol, nrow, ilay
99
            h = ff.readReals()
101
    ff.close()
102
103
   xmin, xmax = (601700.0, 630000.0)
104
   ymin, ymax = (3566500.0, 3597100.0)
105
   hmin = min(h)
106
   hmax = max(h)
107
108
   # write output in Surfer ASCII grid format
109
   f = open('modeled_head_asciihed.grd','w')
110
   f.write("""DSAA
111
   %i %i
   %.1f %.1f
   %.1f %.1f
   %.8e %.8e
   """ %(ncol, nrow, xmin, xmax, ymin, ymax, hmin, hmax) )
   hmat = reshapev2m(h, ncol, nrow)
117
118
   # MODFLOW starts data in upper-left corner
119
   \# Surfer expects data starting in lower-left corner
120
   # flip array in row direction
121
122
   floatmatsave(f,hmat[::-1])
123
   f.close()
124
```

#### A-4.9 Python script merge\_observed\_modeled\_heads.py

```
fobs = open('meas_head_2009ASER.smp','r') # measured head
                                                 # modeled head
   fmod = open('modeled_head.smp','r')
   fwgt = open('obs_loc_2009ASER.dat','r')
                                                  \# weights
                                                  \# x/y \ coordinates
   fdb = open('spec_wells.crd','r')
   fout = open('both_heads.smp','w')
                                                  # resulting file
   \# read in list of x/y coordinates, key by well name
   wells = \{\}
9
   for line in fdb:
10
        well, x, y = line.split()[0:3] \# ignore last column
        wells[well.upper()] = [x,y]
   fdb.close()
13
14
   fout.write('\t'.join(['\#NAME','UTM-NAD27-X','UTM-NAD27-Y','OBSERVED','MODELED','OBS-MOD','WEIGHT'])+'\n')
15
16
17
   for sobs, smod, w in zip(fobs, fmod, fwgt):
18
        obs = float(sobs.split()[3])
19
       mod = float (smod.split()[3])
20
       name = sobs.split()[0].upper()
21
       fout.write('\t'.join([name, wells [name][0], wells [name][1],
22
                                str(obs), str(mod), str(obs-mod),
23
                                w.rstrip().split()[1]])+'\n')
24
   fobs.close()
   fmod.close()
   fwgt.close()
   fout.close()
```

#### A-4.10 Python script convert\_dtrkmf\_output\_for\_surfer.py

```
\# grid origin for dtrkmf cell \rightarrow x, y conversion
  x0 = 601700.0
  y0 = 3597100.0
  dx = 100.0
   dv = 100.0
   fout = open('dtrk_output.bln','w')
10
   # read in all results for saving particle tracks
11
   fin = open('dtrk.out','r')
   results = [1.split() for 1 in fin.readlines()[1:]]
   fin.close()
14
15
   npts = len(results)
16
17
  # write Surfer blanking file header
18
   fout.write('%i,1\n' % npts)
19
20
   \# write x, y location and time
21
   for pt in results:
       x = float(pt[1])*dx + x0
       y = y0 - float(pt[2])*dy
       t = float(pt[0])/7.75*4.0  # convert 7.75m to 4m Cuelbra thickness
       fout.write('\%.1f,\%.1f,\%.8e\n'\% (x,y,t))
   fout.close()
```